The Second Derivative

1. Laura says:

I feel bad today, but I'm feeling better than yesterday, and I seem to be improving faster and faster.

Let f(t) be Laura's health as a function of time. Based on her statement, what can you say about the signs of f(t), f'(t), and f''(t)?

2. Representative Michaud says:

The defense budget will increase this year, but not by as much as it increased last year.

Let B(t) be the defense budget as a function of time. Based on Congressman Michaud's remarks, what can you say about the signed of B'(t) and B''(t)?

- 3. Let f(t) be the number of inches of rain that has fallen since midnight, where t is the time in hours. Interpret the following in practical terms, giving units.
 - (a) f(10) = 1.4(b) f'(1) = 0.1(c) f''(10) = -0.2(d) $f^{-1}(1) = 3$ (e) $(f^{-1})'(1.4) = 3$
- 4. Sketch a graph of a function that has the following properties: Its second derivative is positive everywhere and the first derivative is negative if x < -2 and positive if x > -2.
- 5. Sketch a graph of a function that has the following properties: Its second derivative is positive everywhere and the first derivative is positive if x < -2 and negative if x > -2.

- 6. The plot below is of a f'(x). For what values of x is:
 - (a) f(x) increasing?
 - (b) f(x) decreasing?
 - (c) f'(x) positive?
 - (d) f'(x) negative?
 - (e) f''(x) positive?
 - (f) f''(x) negative?
- 7. Sketch f''(x), given the f'(x) in Fig. 1.
- 8. Sketch a possible f(x) that corresponds to the f'(x) in Fig. 1.

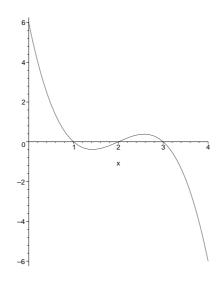


Figure 1: A plot of f'(x).