Using the Derivative: Minima and Maxima

1. Analyze the following function. Find and classify all critical points. Find all inflection points. Determine any local maxima or minima (x and y values). Sketch the function.

$$g(x) = -x^2 + 6x - 5.$$
 (1)

2. In the figure is show a plot of a function's derivative. Find and classify all critical points. Find any inflection points. Sketch f(x).



3. Analyze the following function. Find and classify all critical points. Find all inflection points. Determine any local maxima or minima (x and y values). Sketch the function.

$$h(x) = x + \sin(x) \tag{2}$$

4. Suppose you can chose any two numbers, so long as they add up to 8. What should those two numbers be to make their product is as large as possible?