Chapter 4.3: Optimization Calculus I

College of the Atlantic. Fall 2016

1. Let $g(x) = x^2 - 6x + 11$.

- (a) What is the global minimum and maximum of g(x) on the interval [1, 4]?
- (b) What is the global minim and maximum of g(x) on the interval [3, 4]?
- 2. Consider $f(x) = xe^{-x^4}$, where x is always greater or equal to zero. What is the maximum value of f(x)? What is the minimum value?
- 3. Sketch a continuous function that has local minima at 2 and 4, a global maximum at 3, and no other extrema.
- 4. Sketch a continuous function that has no critical points but has an inflection point at x = -2.
- 5. In the figure is shown a plot of the cost of running a school as a function of the number of students. What number of students leads to the lowest average cost per student?



6. A grapefruit is tossed straight up with an initial velocity of 50 ft/s. The grapefruit is 5 feet above the ground when it is released. Its height at time t is given by

$$h(t) = -16t^2 + 50t + 5.$$
 (1)

- (a) How high does it go before returning to the ground?
- (b) How long does it take the grapefruit to reach its maximum height?