## Homework Six Calculus I College of the Atlantic

## Due Friday, October 25, 2024

There are two parts to this assignment.

**Part 1: WeBWorK**. Do Homework 06A and 06B on WeBWorK. The WeBWorK page is here: https://webwork-hosting.runestone.academy/webwork2/coa-feldman-es1024-fall2024 I recommend doing the WeBWorK part of the homework first. This will enable you to benefit WeBWorK's instant feedback before you do part two.

**Part 2: Non-WeBWorK problems**. Here are some instructions for how to submit this part of the assignment.

- Do the problems by hand using pencil (or pen) and paper. There is no need to type this assignment.
- Make a pdf scan of your work using genius scan or some similar scanning app. Please make the homework into a single pdf, not multiple pdfs.
- Submit the assignment on google classroom. Please don't email it to me.
- If you want, you can do the non-WeBWorK problems in pairs and submit only one assignment for the two of you.

Here are some non-WeBWorK problems.

1. The temperature T of an object as a function of time is described by the following function:

$$T(t) = 20 + 40e^{-kt} , (1)$$

where k = 0.003, t is measured in seconds, and temperature is measured in Celsius.

(a) Sketch T(t).

- (b) What is the initial temperature of the object?
- (c) What is the temperature of the object after a long time (as t gets very large)?
- (d) At what time is the temperature 30 Celsius?
- (e) At t = 200, at what rate is the object cooling?

- 2. Consider the function  $f(x) = xe^x$ .
  - (a) For what values of x is f(x) concave up? Figure this out by taking two derivative of f(x) and then determining what range of x values makes the second derivative positive.
  - (b) Sketch the function using limits that make it clear where the concavity changes.

3. (Hint: Thinking about units will be very helpful.) Let f(v) be the gas consumption in liters/km of a car going at a speed v, measured in km/h4. This means that f(v) tells you how many liters of gas the car uses to go one kilometer when it is traveling at a speed of v. Suppose we know that

$$f(80) = 0.05$$
, and  $f'(80) = 0.0005$ . (2)

- (a) Let g(v) be the distance the same car gravels on one liter of gas if it is traveling at speed v.
  - i. How are f(v) and g(v) related? (Your answer should be an equation.)
  - ii. Determine g(80) and g'(80).
  - iii. What is the practical meaning of g'(80)?
- (b) Let h(v) be the gas consumption in liters per hour. So h(v) tells you how many liters of gas the car uses in one hour if it is traveling at a speed of v.
  - i. How are f(v) and h(v) related? (Your answer should be an equation.)
  - ii. Determine h(80) and h'(80).
  - iii. What is the practical meaning of h'(80)?