

Substitutions

1. Find the following anti-derivatives:

$$\int t \cos(t^2) dt \quad (1)$$

$$\int x^2(x^3 - 3) dx \quad (2)$$

$$\int (x^2 + 3)^2 dx \quad (3)$$

$$\int \sqrt{\cos(3t)} \sin(3t) dt \quad (4)$$

$$\int \frac{1}{2x} dx \quad (5)$$

2. Find the following definite integrals:

$$\int_0^{\frac{1}{2}} \cos(\pi x) dx \quad (6)$$

$$\int_1^2 2xe^{x^2} dx \quad (7)$$

$$\int_0^2 \frac{x}{(1+x^2)^2} dx \quad (8)$$