

Chapter C12: Power

Physics I

College of the Atlantic

C12.1: Power

Power in physics is defined as rate of energy transfer—energy per time.

$$\text{Power} \equiv \frac{|\Delta\text{Energy}|}{\Delta\text{time}} . \quad (1)$$

The unit of power is the *Watt*;

$$1\text{Watt} \equiv 1\text{J/s} \quad (2)$$

Power companies measure energy in units of *kilowatt hours*

$$1\text{kWh} = 3.6\text{MJ} . \quad (3)$$

One kilowatt hour is the amount of energy that is transferred if one kilowatt of power is delivered for one hour.

Examples:

1. You need a heater that can raise the temperature of water 30° C in 15 minutes. What power must the heater be capable of delivering?
2. How much does it cost in Maine to run 2000 Watt electric heater for 8 hours? How much would this cost per month?

Some handy info

- Conversion Factors:

$$1\text{kWh} = 3.6 \text{ MJ} . \quad (4)$$

$$746 \text{ Watts} = 1 \text{ horsepower} . \quad (5)$$

- The average US energy consumption: 250 kWh per person per day.
- An electric dryer draws around 3 kilowatts.
- A toaster draws around 1000 Watts.
- A kWh of electrical energy costs \$0.17 in Maine.
- A kWh of electricity in Maine leads to roughly 300g of CO₂ being emitted into the atmosphere.
- A typical Maine home uses around 500 kWh of electricity a month.
- A typical solar cell in Maine generates around 10W of electrical power per m² of solar cell.

C13.2: Cross Product

The cross product is, like the dot product, a way to “multiply” two vectors together. The dot product takes two vectors and turns them into a scalar. The cross product takes two vectors and returns another vector.

$$\text{mag}(\vec{u} \times \vec{w}) = uw \sin \theta \quad (6)$$

A more physical/geometric way to think of this is:

$$\text{mag}(\vec{u} \times \vec{w}) = uw_{\perp} = u_{\perp}w. \quad (7)$$

The direction of $\vec{u} \times \vec{w}$ is perpendicular to the plane that contains \vec{u} and \vec{w} and is given by the right hand rule.

In components:

$$\vec{u} \times \vec{w} \equiv \begin{bmatrix} u_y w_z - u_z w_y \\ u_z w_x - u_x w_z \\ u_x w_y - u_y w_x \end{bmatrix} \quad (8)$$

We won't use this equation explicitly, but it is perhaps comforting to know that it exists. Or maybe not. Anyway...

Note that $\vec{u} \times \vec{v} = -\vec{v} \times \vec{u}$.

Examples

- Let \vec{u} be a displacement vector of 2 meters that points due east, and let \vec{w} be a vector with a magnitude of 3 meters that points due south.
 - Find $\vec{u} \times \vec{w}$.
 - Find $\vec{u} \cdot \vec{w}$.
 - Find $\vec{u} \cdot \vec{u}$.
 - Find $\vec{u} \times \vec{u}$.
- Let \vec{v}_1 be a displacement vector of 3 meters that points due east, and let \vec{v}_2 be a vector with a magnitude of 2 meters that points 60 degrees north of east.
 - Find $\vec{v}_1 \times \vec{v}_2$.
 - Find $\vec{v}_1 \cdot \vec{v}_2$.
- Let \vec{a} be a displacement vector of 3 meters that points due east, and let \vec{b} be a vector with a magnitude of 2 meters that points due west.
 - Find $\vec{a} \times \vec{b}$.
 - Find $\vec{a} \cdot \vec{b}$.