# C7 Potential Energy

### C7.1: The Electromagnetic Interaction

Don't worry much about this section.

#### C7.2: The Gravitational Interaction

The main equation:

$$V(r) = -G\frac{m_1 m_2}{r} \,. \tag{1}$$

This looks weird. Sketch the function and remember that all that matters is potential energy differences. Then it won't seem so bad.

#### C7.3: Gravitation Near the Earth

The punchline of this section is Figure C7.3 on p. 123. This figure shows us that Eq. (1) is well approximated by V(z) = mgz near the earth's surface.

## C7.4: The Potential Energy of a Spring

The main equation:

$$V(r) = \frac{1}{2}k_s(r - r_0)^2 . (2)$$

This is often written in the simpler form:

$$V(r) = \frac{1}{2}k_s x^2 \,, \tag{3}$$

where it is understood that the spring has zero potential energy when it is relaxed—i.e. neither compressed or stretched.

### C7.5: Examples

# C7.6: Significant Digits

Don't get carried away with digits.

#### Practice

- 1. A 50 kg diver jumps into the sea 40 meters below. The water into which she jumps is 20 meters deep. Determine her speed immediately before she hits the water. Do this problem two ways:
  - (a) Use the surface of the water as your reference level.
  - (b) Use the bottom of the sea as your reference level.
- 2. The space shuttle orbits at an altitude of 400 km above the earth's surface. Suppose the shuttle suddenly stops orbiting and falls to earth. What is the speed of the shuttle right before it hits the earth's surface? Ignore air friction. Do this problem two ways:
  - (a) Use formula C7.3 for the gravitational potential energy
  - (b) Use V(z) = mgz for the gravitational potential energy
- 3. A spring with a spring constant of  $300 \text{ J/m}^2$  is compressed 3 cm. This is then used to shoot a 30 g marble straight up into the air.
  - (a) What is the marble's speed immediately after the spring is released and before it begins its upward trajectory.
  - (b) How high will the marble go?
  - (c) What is the marble's speed when it's at half of its maximum height?
- 4. You would like to get a spring that is springey enough to launch your friend 2 meters into the air. What strength spring should you buy?